



GGSRDN

Educational Services Private Limited

9th, 10th, NEET, JEE (Main/Advanced)

अभ्यास ही सबसे बड़ा गुरु है।

CLASS : XI (MATHS)

DPP

DAILY PRACTICE PROBLEM

DPP-11 to 20

DPP 11 : Fundamentals of Mathematics, Quadratic Equation, Complex Number

DPP 12 : Fundamentals of Mathematics, Quadratic Equation, Parabola

DPP 13 : Fundamentals of Mathematics, Quadratic Equation

DPP 14 : Quadratic Equation

DPP 15 : Quadratic Equation

DPP 16 : Quadratic Equation

DPP 17 : Fundamentals of Mathematics

DPP 18 : Fundamentals of Mathematics, Quadratic Equation

DPP 19 : Sets & Relation, Sequence & Series

DPP 20 : Sequence & Series

MATHEMATICS

DPP

DAILY PRACTICE PROBLEMS

DPP No. 11

Total Marks : 29

Max. Time : 31 min.

Topics : Fundamentals of Mathematics, Quadratic Equation, Complex Number

Type of Questions

		M.M.,	Min.
Comprehension (no negative marking) Q.1 to Q.3	(3 marks, 3 min.)	[9,	9]
Single choice Objective (no negative marking) Q.4, 5, 6, 7	(3 marks, 3 min.)	[12,	12]
Subjective Questions (no negative marking) Q.8,9	(4 marks, 5 min.)	[8,	10]

COMPREHENSION (Q. No. 1 to 3)

Consider the equation $|2x - 1| - 2|x - 2| = \lambda$

- If the above equation has only one solution, then λ belongs to
 (A) $\{-3, 3\}$ (B) $[-3, 3]$ (C) $(-3, 3)$ (D) ϕ
- If the above equation has more than one solutions then λ belongs to
 (A) $\{-3, 3\}$ (B) $[-3, 3]$ (C) $(-3, 3)$ (D) ϕ
- If $\lambda = 6$, then the above equation has
 (A) only one solution (B) only two solutions. (C) no solution. (D) more than two solutions.
- If the roots of the equation $x^2 + 2cx + ab = 0$ are real and unequal, then the roots of the equation $x^2 - 2(a + b)x + (a^2 + b^2 + 2c^2) = 0$ are :
 (A) real and unequal (B) real and equal
 (C) imaginary (D) rational
- If $-3 + 5i$ is a root of the equation $x^2 + px + q = 0$, then the ordered pair (p, q) is $(p, q \in \mathbb{R})$
 (A) $(-6, 34)$ (B) $(6, 34)$ (C) $(34, -6)$ (D) $(34, 6)$
- If the quadratic equation $ax^2 + bx + a^2 + b^2 + c^2 - ab - bc - ca = 0$, where a, b, c are distinct reals, has imaginary roots then :
 (A) $2(a - b) + (a - b)^2 + (b - c)^2 + (c - a)^2 > 0$
 (B) $2(a - b) + (a - b)^2 + (b - c)^2 + (c - a)^2 < 0$
 (C) $2(a - b) + (a - b)^2 + (b - c)^2 + (c - a)^2 = 0$
 (D) none
- If the quadratic equations $ax^2 + 2cx + b = 0$ & $ax^2 + 2bx + c = 0$ ($b \neq c$) have a common root, then $a + 4b + 4c$ is equal to :
 (A) -2 (B) -2 (C) 0 (D) 1
- Solve the equation : $|x+1| - |x| + 3|x-1| - 2|x-2| = x+2$
- Solve the equation : $\left| \frac{x+1}{x} \right| + |x+1| = \frac{(x+1)^2}{x}$

MATHEMATICS

DPP

DAILY PRACTICE PROBLEMS

DPP No. 12

Total Marks : 30

Max. Time : 30 min.

Topics : Fundamentals of Mathematics, Quadratic Equation, Parabola

Type of Questions

Type of Questions	M.M.,	Min.
Comprehension (no negative marking) Q.1 to Q.3	(3 marks, 3 min.)	[9, 9]
Single choice Objective (no negative marking) Q.4, 5, 6, 7	(3 marks, 3 min.)	[12, 12]
Multiple choice objective (no negative marking) Q. 8	(5 marks, 4 min.)	[5, 4]
Subjective Questions (no negative marking) Q.9	(4 marks, 5 min.)	[4, 5]

COMPREHENSION (For Q.No. 1 to 3)

The coordinates of the vertex of the parabola $f(x) = 2x^2 + px + q$ are $(-3, 1)$, then

- The value of p is
(A) 12 (B) -12 (C) 19 (D) -19
- The value of q is
(A) -19 (B) 19 (C) -12 (D) none of these
- The parabola
(A) touches the x -axis (B) intersect the x -axis in two real and distinct points
(C) lies completely above the x -axis (D) lies completely below the x -axis
- The solution set of the inequation $\left| \frac{1}{x} - 2 \right| < 4$, is
(A) $(-\infty, -1/2)$ (B) $(1/6, \infty)$ (C) $(-1/2, 1/6)$ (D) $(-\infty, -1/2) \cup (1/6, \infty)$
- Minimum value of $f(x) = 2x^2 - 4x + 5$ is
(A) 1 (B) -1 (C) 11 (D) 3
- The least integral value of ' m ' for which the expression $m^2 - 4x + 3m + 1$ is positive for every $x \in \mathbb{R}$ is :
(A) 1 (B) -2 (C) -1 (D) 2
- The least integral value of ' a ' for which the graphs $y = 2ax + 1$ and $y = (a - 6)x^2 - 2$ do not intersect
(A) -6 (B) -5 (C) 3 (D) 2
- If the quadratic equations $x^2 - 5x + 4 = 0$ and $x^2 - 6x + k = 0$ have one common root, then ' k ' is equal to
(A) 4 (B) 8 (C) 3 (D) 5

9. Match the following

Consider the parabola $f(x) = x^2 + kx + 4$

Column - I

- (A) Curve intersects the x -axis for
(B) Curve touches the x -axis for
(C) Curve neither intersect nor touches the x -axis for
(D) $f(x) > 0 \forall x \in \mathbb{R}$ for

Column - II

- (p) $k \in (-\infty, -4) \cup (4, \infty)$
(q) $k \in (-4, 4)$
(r) $k \in \{-4, 4\}$

MATHEMATICS

DPP

DAILY PRACTICE PROBLEMS

DPP No. 13

Total Marks : 24

Max. Time : 27 min.

Topics : Fundamentals of Mathematics, Quadratic Equation

Type of Questions

Type of Questions	M.M., Min.
Comprehension (no negative marking) Q.1 to Q.3	(3 marks, 3 min.) [9, 9]
Single choice Objective (no negative marking) Q.4	(3 marks, 3 min.) [3, 3]
Subjective Questions (no negative marking) Q.5,6,7	(4 marks, 5 min.) [12, 15]

COMPREHENSION (For Q.No. 1 to 3)

Let $y = ax^2 + bx + c$ be a quadratic expression having its vertex at $(3, -2)$ and value of $c = 10$, then

- Value of 'b' is equal to
 (A) 6 (B) -6 (C) 8 (D) -8
- One of the roots of the equation $ax^2 + bx + c = 0$ is
 (A) $\frac{6 + \sqrt{6}}{2}$ (B) $\frac{3 + \sqrt{6}}{2}$ (C) $3 - \sqrt{6}$ (D) $3 + \sqrt{6}$
- If $y \geq -\frac{2}{3}$, then
 (A) $x \in (-\infty, 2] \cup [4, \infty)$ (B) $x \in (-\infty, 3] \cup [4, \infty)$
 (C) $x \in (-\infty, 1] \cup [3, \infty)$ (D) $x \in (-\infty, 4] \cup [6, \infty)$
- Find the set of values of ' α ' for which the expression $y = \frac{\alpha x^2 + 6x - 8}{\alpha + 6x - 8x^2}$ have a common linear factor in numerator and denominator
 (A) {14} (B) {2} (C) {-8, 2, 14} (D) {0, 2, 14}
- Solve the following equations $x^2 + xy + xz = 18$, $y^2 + yz + yx + 12 = 0$ and $z^2 + zx + zy = 30$
- Solve the following inequations
 (i) $(x - 5)(x + 9)(x - 8) < 0$ (ii) $x^2 - 4x + 9 > 0$
 (iii) $x^4 - 5x^2 + 4 < 0$ (iv) $\frac{3}{x - 2} < 1$
- Consider the quadratic polynomial, $f(x) = x^2 - 4ax + 5a^2 - 6a$.
 (a) Find the smallest positive integral value of 'a' for which $f(x)$ is positive for every real x.
 (b) Find the largest distance between the roots of the equation $f(x) = 0$.

Topic : Quadratic Equation

Type of Questions

M.M., Min.

Single choice Objective (no negative marking) Q.1,2,3,4, 5

(3 marks, 3 min.)

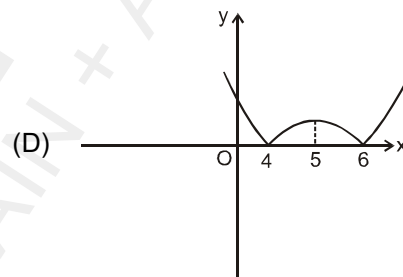
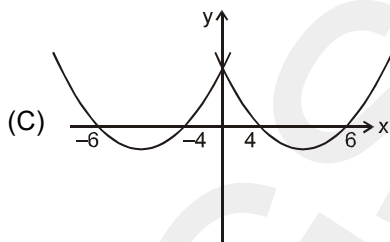
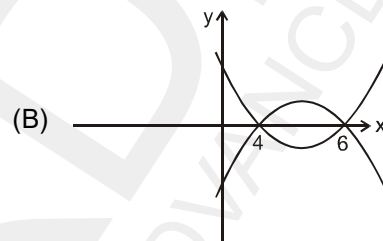
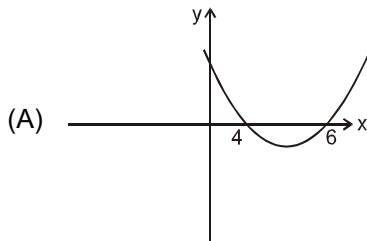
[15, 15]

Subjective Questions (no negative marking) Q.6,7

(4 marks, 5 min.)

[8, 10]

1. Which of the following is the graph of $y = |x^2 - 10x + 24|$



2. Solution set of the equation $3^{2x^2} - 2 \cdot 3^{x^2+x+6} + 3^{2(x+6)} = 0$ is

(A) $\{-3, 2\}$

(B) $\{6, -1\}$

(C) $\{-2, 3\}$

(D) $\{1, -6\}$

3. The set of values of 'a' for which both roots of the equation $x^2 + 2(a + 1)x + (9a - 5) = 0$ are negative is :

(A) $[0, \infty)$

(B) $(-\infty, 6]$

(C) $(-\infty, 0]$

(D) $\left[\frac{5}{9}, 1\right] \cup [6, \infty)$

4. The set of all values of 'a' for which the quadratic equation $3x^2 + 2(a^2 + 1)x + (a^2 - 3a + 2) = 0$ possess roots of opposite sign, is

(A) $(-\infty, 1)$

(B) $(-\infty, 0)$

(C) $(1, 2)$

(D) $(3/2, 2)$

5. If roots of equation $x^2 - 2mx + m^2 - 1 = 0$ lie in the interval $(-2, 4)$, then

(A) $m \in (-1, 3)$

(B) $m \in (1, 5)$

(C) $m \in (1, 3)$

(D) $m \in (-1, 5)$

6. Find the equation each of whose roots is greater by unity, than the roots of the equation $x^3 - 5x^2 + 6x - 3 = 0$.

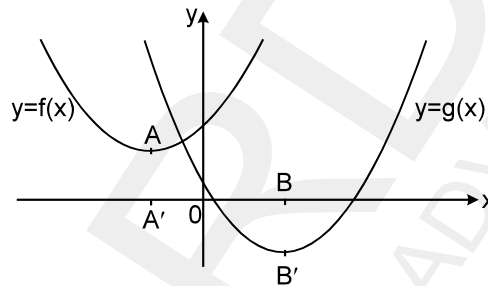
7. Find all values of 'p' for which the root(s) of the equation $(p - 3)x^2 - 2px + 5p = 0$ are real and positive

Topic : Quadratic Equation

Type of Questions		M.M., Min.
Comprehension (no negative marking) Q.1 to Q.3	(3 marks, 3 min.)	[9, 9]
Single choice Objective (no negative marking) Q.4,5,6	(3 marks, 3 min.)	[9, 9]
Subjective Questions (no negative marking) Q.7	(4 marks, 5 min.)	[4, 5]

COMPREHENSION (For Q.No. 1 to 3)

Let $f(x) = x^2 + 2ax + b$, $g(x) = cx^2 + 2dx + 1$ be quadratic expressions whose graph is as shown in the figure



Here it is given that $|AA'| = |BB'|$ and $|OA'| = |OB|$.

- Which of the following statements is correct
 (A) $a^2 + d = d^2 + c$ (B) $a + d = b + c$ (C) $a^2 + d^2 = c + b$ (D) $bc + c = a^2c + d^2$
- Sum of roots of equations $f(x) = 0$ and $g(x) = 0$ is
 (A) 0 (B) $2(a + d)$ (C) $1 + b$ (D) $2a - \frac{2d}{c}$
- If $|OA'| = |AA'| = 1$, then the values of 'm' for which $(g(x))^2 + mg(x) + 4 = 0$ has two real roots which are distinct
 (A) (0, 4) (B) (4, ∞) (C) (4, 5) (D) (5, ∞)
- If α & β are the roots of the quadratic equation $ax^2 + bx + c = 0$, then the quadratic equation, $ax^2 - bx(x - 1) + c(x - 1)^2 = 0$ has roots :
 (A) $\frac{\alpha}{1-\alpha}, \frac{\beta}{1-\beta}$ (B) $\alpha - 1, \beta - 1$ (C) $\frac{\alpha}{\alpha+1}, \frac{\beta}{\beta+1}$ (D) $\frac{1-\alpha}{\alpha}, \frac{1-\beta}{\beta}$
- If α, β, γ are the roots of the equation $x^3 - px^2 + qx - r = 0$, then the value of $\sum \alpha^2\beta$ is equal to
 (A) $pq + 3r$ (B) $pq + r$ (C) $pq - 3r$ (D) q^2/r
- If α, β, γ are the roots of the equation $x^3 - px^2 + qx - r = 0$, then the value of $\left(\frac{1}{\alpha^2} + \frac{1}{\beta^2} + \frac{1}{\gamma^2}\right)$ is :
 (A) $\frac{p^2 - 2qr}{r^2}$ (B) $\frac{q^2 - 2pr}{r^2}$ (C) $\frac{r^2 - 2pq}{r^2}$ (D) none of these
- Find all values of 'k' for which the inequality $(x - 3k)(x - k - 3) < 0$ is true $\forall x \in [1, 3]$.

Topic : Quadratic Equation

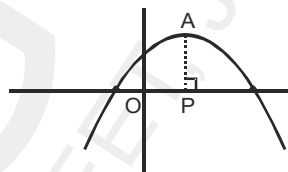
Type of Questions

		M.M., Min.
Comprehension (no negative marking) Q.1 to 3	(3 marks, 3 min.)	[9, 9]
Single choice Objective (no negative marking) Q.4,5,6,7	(3 marks, 3 min.)	[12, 12]
Subjective Questions (no negative marking) Q.8	(4 marks, 5 min.)	[4, 5]

COMPREHENSION (Q.No. 1 to 3)

Consider the equation $|x^2 - 2x - 3| = m$, $m \in \mathbb{R}$

- If the given equation has four solutions, then
 (A) $m \in (0, \infty)$ (B) $m \in (-1, 3)$ (C) $m \in (0, 4)$ (D) none of these
- If the given equation has three solutions, then
 (A) $m \in (0, \infty)$ (B) $m \in \{4\}$ (C) $m \in (0, 4)$ (D) $m \in (-1, 3)$
- If the given equation has two solutions, then
 (A) $m \in [4, \infty)$ (B) $m \in (-1, 3)$ (C) $m \in (4, \infty) \cup \{0\}$ (D) $m = 0$
- Let a, b, c be three roots of the equation $x^3 + x^2 - 333x - 1002 = 0$, then $(\sum (a^3) - 2 \sum a)$ is equal to
 (A) 2008 (B) 2000 (C) 2006 (D) 2002
- Number of real solutions of the equation $x^2 + \left(\frac{x}{x-1}\right)^2 = 8$ is
 (A) 3 (B) 4 (C) 6 (D) 0
- If $y = ax^2 + bx + c$ represents the curve given in the figure and $b^2 = 2(b + 2ac)$, where $a \neq 0$ and $AP = 3$ units, then $OP =$



- (A) $\frac{3}{2}$ (B) $\frac{3}{4}$ (C) 3 (D) 6
- If $mx^2 - 9mx + 5m + 1 > 0, \forall x \in \mathbb{R}$, then m lies in the interval
 (A) $\left(-\frac{4}{61}, 0\right)$ (B) $\left[0, \frac{4}{61}\right)$ (C) $\left(\frac{4}{61}, \frac{61}{4}\right)$ (D) $\left(-\frac{61}{4}, 0\right)$
- Find the range of values of 'a' such that $f(x) = \frac{ax^2 + 2(a+1)x + 9a + 4}{x^2 - 8x + 32}$ is always negative?

MATHEMATICS

DPP

DAILY PRACTICE PROBLEMS

DPP No. 17

Total Marks : 58

Max. Time : 71 min.

Topic : Fundamentals of Mathematics

Type of Questions

		M.M.,	Min.
Single choice Objective (no negative marking) Q.11, 12	(3 marks, 3 min.)	[6,	6]
Subjective Questions (no negative marking) Q.1 to 10 and 13,14,15	(4 marks, 5 min.)	[52,	65]

Solve the following inequality

1. $|x - 3| < 5$

2. $2 \leq |x - 1| \leq 3$

3. $|x - 1| \leq 5$ and $|x| \geq 2$

4. $|x - 1| + |x - 2| \geq 4$

5. $\frac{|x|+1}{|x|-2} \geq 0, x \in \mathbb{R}, x \neq \pm 2$

6. $\frac{-1}{|x|-2} \geq 1, \text{ where } x \in \mathbb{R}, x \neq \pm 2$

7. $\frac{|x+3|+x}{x+2} > 1$

8. $||x - 2| - 1| \geq 3$

9. $|(x^2 + 2x + 2) + (3x + 7)| < |x^2 + 2x + 2| + |3x + 7|$

10. $|x^2 - 1| + |x^2 - 4| \leq 3$

11. The solution of $|x^2 + 3x| + x^2 - 2 \geq 0$ is :

(A) $(-\infty, 1)$

(B) $(0, 1)$

(C) $\left(-\infty, -\frac{2}{3}\right] \cup \left[\frac{1}{2}, \infty\right)$

(D) None of these

12. The solution of $||x| - 1| < |1 - x|, x \in \mathbb{R}$ is :

(A) $(-1, 1)$

(B) $(0, \infty)$

(C) $(-1, \infty)$

(D) None of these

13. Solve : $|x^2 + 4x + 3| + 2x + 5 = 0$

14. Solve $|x^2 - 3x - 4| = 9 - |x^2 - 1|$

15. Solve the inequality $|f(x) - g(x)| < |f(x)| + |g(x)|$, where $f(x) = x - 3$ and $g(x) = 4 - x$

MATHEMATICS

DPP

DAILY PRACTICE PROBLEMS

DPP No. 18

Total Marks : 28

Max. Time : 29 min.

Topics : Fundamentals of Mathematics, Quadratic Equation

Type of Questions

		M.M.,	Min.
Comprehension (no negative marking) Q.1 to 3	(3 marks, 3 min.)	[9,	9]
Single choice Objective (no negative marking) Q.4,5	(3 marks, 3 min.)	[6,	6]
Multiple choice objective (no negative marking) Q.6	(5 marks, 4 min.)	[5,	4]
Subjective Questions (no negative marking) Q.7,8	(4 marks, 5 min.)	[8,	10]

COMPREHENSION (For Q.1 to 3)

Consider the equation $||x - 1| - 2| = \lambda$

- If the given equation has two solutions, then λ belongs to
 (A) $(2, \infty) \cup \{0\}$ (B) $(2, \infty)$ (C) $(0, 2)$ (D) none of these
- If the given equation has three solutions, then λ belongs to
 (A) $(0, 2)$ (B) $\{2\}$ (C) $(0, \infty)$ (D) $(-\infty, 0)$
- Number of integral values of λ so that the given equation has four solutions, is
 (A) 0 (B) 1 (C) 2 (D) 3
- If α, β, γ are the roots of the equation $x^3 - px^2 + qx - r = 0$, then the value of $\sum \frac{\alpha\beta}{\gamma}$ is equal to
 (A) $pq + 3r$ (B) $pq + r$ (C) $pq - 3r$ (D) $\frac{q^2 - 2pr}{r}$
- S_1 : For $ax^2 + bx + c = 0$ ($a \neq 0$) if $a + b + c = 0$, then the roots are 1 and c/a

S_2 : If $f(x) = ax^2 + bx + c$ ($a \neq 0$) has finite minimum value and both roots are of opposite sign, then $f(0) < 0$

S_3 : If α is repeated root of $ax^2 + bx + c = 0$, $a \neq 0$, then $ax^2 + bx + c = (x - \alpha)^2$

S_4 : For $ax^2 + bx + c = 0$ ($a \neq 0$), irrational roots occur in conjugate pairs only

State in order, whether S_1, S_2, S_3, S_4 are true or false
 (A) TFTF (B) TTFF (C) FTFT (D) TTTT
- If α, β are the roots of the equation $x^2 + \alpha x + \beta = 0$ such that $\alpha \neq \beta$ and $||x - \beta| - \alpha| < \alpha$, then
 (A) inequality is satisfied by exactly two integral values of x
 (B) inequality is satisfied by all values of $x \in (-4, -2)$
 (C) Roots of the equation are opposite in sign
 (D) $x^2 + \alpha x + \beta < 0 \forall x \in [-1, 0]$
- Find the set of values of 'a' for which the roots of the quadratic equation
 $(a - 5)x^2 + (\sqrt{4a - a^2})x + (a^2 - 2a - 3) = 0$ are of opposite sign.
- If inequality $\frac{ax^2 + 3x + 4}{x^2 + 2x + 2} < 5$ is satisfied for all real values of x then find out greatest integral value of 'a'.

MATHEMATICS

DPP

DAILY PRACTICE PROBLEMS

DPP No. 19

Total Marks : 23

Max. Time : 22 min.

Topics : Sets & Relation, Sequence & Series

Type of Questions

M.M., Min.

Single choice Objective (no negative marking) Q.1,2,3,4,5,6,

(3 marks, 3 min.)

[18, 18]

Multiple choice objective (no negative marking) Q.7

(5 marks, 4 min.)

[5, 4]

- In a certain town 25% families own a phone and 15% own a car, 65% families own neither a phone nor a car. 2000 families own both a car and a phone. Consider the following statements in this regard :
 - 10% families own both a car and a phone.
 - 35% families own either a car or a phone.
 - 40,000 families live in the town.
 Which of the above statements are correct ?
 (A) 1 and 2 (B) 1 and 3 (C) 2 and 3 (D) 1, 2 and 3
- $A \cap (B \cup A)'$ =
 (A) ϕ (B) A (C) B (D) $A \cap B$
- In a school there are 20 teachers who teach mathematics or physics. Of these, 12 teach mathematics and 4 teach both physics and mathematics, the number of teachers who teach physics are-
 (A) 12 (B) 16 (C) 8 (D) 4
- Sum of all the odd numbers between 1 and 1000 which are divisible by 3 is
 (A) 83667 (B) 167334 (C) 82667 (D) 166334
- Let a_n be the n^{th} term of an A.P. If $\sum_{r=1}^{100} a_{2r} = \alpha$ & $\sum_{r=1}^{100} a_{2r-1} = \beta$, then the common difference of the A.P. is
 (A) $\alpha - \beta$ (B) $\beta - \alpha$ (C) $\frac{\alpha - \beta}{2}$ (D) none of these
- The ratio of sums of n -terms of two arithmetic progressions is $(3n - 13) : (5n + 21)$. The ratio of 24th term of the two series is :
 (A) 59 : 141 (B) 7 : 17 (C) 1 : 2 (D) none of these
- The sum of the first three consecutive terms of an A.P. is 9 and the sum of their squares is 35. Then sum to n terms of the series is :
 (A) $n(n + 1)$ (B) n^2 (C) $n(4 - n)$ (D) $n(6 - n)$

MATHEMATICS

DPP

DAILY PRACTICE PROBLEMS

DPP No. 20

Total Marks : 23

Max. Time : 25 min.

Topic : Sequence & Series

Type of Questions

		M.M.,	Min.
Comprehension (no negative marking) Q.1 to Q.3	(3 marks, 3 min.)	[9,	9]
Single choice Objective (no negative marking) Q.4,5	(3 marks, 3 min.)	[6,	6]
Subjective Questions (no negative marking) Q.6,7	(4 marks, 5 min.)	[8,	10]

COMPREHENSION (Q.No. 1 to 3)

Given a special sequence a, b, c, d such that first three numbers are in A.P. while the last three are in G.P. If

the first number is 18 and common ratio of G.P. is $\frac{1}{2}$, then answer the following questions.

- The value of $c + d$ is given by
 (A) 9 (B) 10 (C) 11 (D) 12
- If three A.M.s are inserted between b and c , then the third A.M. is
 (A) $\frac{11}{2}$ (B) $\frac{13}{2}$ (C) $\frac{15}{2}$ (D) $\frac{17}{2}$
- If four G.M.s are inserted between k_1c and k_2d , where $k_2 = 64k_1$, then the common ratio of G.P. so formed is
 (A) 2 (B) $\frac{3}{2}$ (C) $\frac{2}{3}$ (D) $\frac{1}{3}$
- If the sum of first three terms of a G.P. is to the sum of first six terms as 125 : 152, then the common ratio of the G.P. is
 (A) $\frac{3}{5}$ (B) $\frac{5}{3}$ (C) $\frac{2}{5}$ (D) $\frac{5}{2}$
- 61st term of the H.P. $\frac{4}{3}, \frac{3}{2}, \frac{12}{7}, \dots$ is
 (A) $-\frac{17}{4}$ (B) $\frac{34}{3}$ (C) $\frac{3}{34}$ (D) $-\frac{4}{17}$
- All terms of the arithmetic progression are natural numbers. The sum of its nine consecutive terms, beginning with the first, is larger than 200 and smaller than 220. Find the progression, if its second term is equal to 12.
- Let x_1 & x_2 be the roots of the equation $x^2 - 3x + A = 0$ and let x_3 & x_4 be the roots of the equation $x^2 - 12x + B = 0$. It is known that the numbers x_1, x_2, x_3, x_4 (in the same order) form an increasing G.P. Find A and B.



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9th, 10th, NEET, JEE (Main/Advanced)

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CLASS : XI (MATHS)

D P P P

DAILY PRACTICE PROBLEM

Solutions

DPP-11 to 20

- DPP 11 : Fundamentals of Mathematics, Quadratic Equation, Complex Number
- DPP 12 : Fundamentals of Mathematics, Quadratic Equation, Parabola
- DPP 13 : Fundamentals of Mathematics, Quadratic Equation
- DPP 14 : Quadratic Equation
- DPP 15 : Quadratic Equation
- DPP 16 : Quadratic Equation
- DPP 17 : Fundamentals of Mathematics
- DPP 18 : Fundamentals of Mathematics, Quadratic Equation
- DPP 19 : Sets & Relation, Sequence & Series
- DPP 20 : Sequence & Series

DPP 11 TO 20 (ANSWER KEY)

DPP NO. - 11

1. (C) 2. (A) 3. (C) 4. (C) 5. (B)
 6. (A)
 7. (C)
 8. $x \in [2, \infty) \cup \{-2\}$
 9. $x \in \{-1\} \cup (0, \infty)$

DPP NO. - 12

1. (A) 2. (B) 3. (C) 4. (D) 5. (D)
 6. (D) 7. (B) 8. (B)(D)
 9. (A) \rightarrow (p), (B) \rightarrow (r), (C) \rightarrow (q), (D) \rightarrow (q)

DPP NO. - 13

1. (D) 2. (A) 3. (A) 4. (C)
 5. $x = 3, y = -2, z = 5$; $x = -3, y = 2, z = -5$
 6. (i) $x \in (-\infty, -9) \cup (5, 8)$ (ii) $x \in (-\infty, \infty)$
 (iii) $x \in (-2, -1) \cup (1, 2)$
 (iv) $x \in (-\infty, 2) \cup (5, \infty)$
 7. (a) 7 (b) 6

DPP NO. - 14

1. (D) 2. (C) 3. (D) 4. (C) 5. (A)
 6. $x^3 - 8x^2 + 19x - 15 = 0$ 7. $p \in \left[3, \frac{15}{4}\right]$

DPP NO. - 15

1. (D) 2. (A) 3. (D) 4. (C)
 5. (C) 6. (B) 7. $k \in \left(0, \frac{1}{3}\right)$

DPP NO. - 16

1. (C) 2. (B) 3. (C) 4. (A) 5. (A)
 6. (C) 7. (B) 8. $a \in \left(-\infty, -\frac{1}{2}\right)$

DPP NO. - 17

1. $x \in (-2, 8)$ 2. $x \in [-2, -1] \cup [3, 4]$
 3. $x \in [-4, -2] \cup [2, 6]$ 4. $x \in \left(-\infty, -\frac{1}{2}\right] \cup \left[\frac{7}{2}, \infty\right)$
 5. $x \in (-\infty, -2) \cup (2, \infty)$ 6. $(-2, -1) \cup [1, 2)$
 7. $x \in [-3, -2) \cup (-1, \infty)$ 8. $(-\infty, -2] \cup [6, \infty)$
 9. $x < -\frac{7}{3}$ 10. $x \in [-2, -1] \cup [1, 2]$
 11. (C) 12. (D) 13. $\{-4, -1, -1 - \sqrt{3}\}$
 14. $\{-2, 2\}$ 15. $x \in (3, 4)$

DPP NO. - 18

1. (A) 2. (B) 3. (B) 4. (D)
 5. (B) 6. (A)(B)(C)(D) 7. $a \in (3, 4]$
 8. 2

DPP NO. - 19

1. (C) 2. (A) 3. (A) 4. (A)
 5. (D) 6. (C) 7. (B)(D)

DPP NO. - 20

1. (A) 2. (C) 3. (A) 4. (A)
 5. (D) 6. 8, 12, 16, 7. $A = 2, B = 32$

5. $\frac{-D}{4a} = \frac{-(16-40)}{8} = 3$

6. $\therefore m > 0$ and $D < 0$
 $16 - 4m(3m + 1) < 0$
 $4 - m(3m + 1) < 0$
 $3m^2 + m - 4 > 0$
 $(3m + 4)(m - 1) > 0$

$m \in \left(-\infty, -\frac{4}{3}\right) \cup (1, \infty)$

But $m > 0$

$\therefore m \in (1, \infty)$

Least integral value = 2

7. $(a-6)x^2 - 2 = 2ax + 1 \Rightarrow (a-6)x^2 - 2ax - 3 = 0$
 $D < 0$

$4a^2 + 12(a-6) < 0$

$a^2 + 3a - 18 < 0$

$(a+6)(a-3) < 0$

$a \in (-6, 3)$

least Integer = -5

8. $\alpha^2 - 5\alpha + 4 = 0 \dots(1)$

$\alpha^2 - 6\alpha + k = 0 \dots(2)$

$-4 - \alpha + k = 0 \Rightarrow k = 4 + \alpha$

from (1) $(k-4)^2 - 5(k-4) + 4 = 0$

$k^2 - 13k + 40 = 0$

$k = 8, 5$

9. $f(x) = x^2 + kx + 4$

(A) $D > 0$

$k^2 > 16$

$k \in (-\infty, -4) \cup (4, \infty)$

(B) $D = 0$

$k^2 = 16$

$k = \pm 4$

(C) $D < 0$

$k \in (-4, 4)$

(D) $f(x) > 0 \forall x \in \mathbb{R}$

$D < 0$

$k \in (-4, 4)$

DPP NO. - 13

1. $v(3, -2), c = 10$

$y = ax^2 + bx + c$

$\frac{-b}{2a} = 3, \frac{4ac - b^2}{4a} = -2$

on solving $b = -8, a = \frac{4}{3}$

so $y = \frac{4}{3}x^2 - 8x + 10$

2. $y = \frac{1}{3}[4x^2 - 24x + 30] = \frac{2}{3}[2x^2 - 12x + 15]$

$x = \frac{6 \pm \sqrt{36 - 30}}{2} = \frac{6 \pm \sqrt{6}}{2}$

3. $y > -\frac{2}{3}$

$\Rightarrow 2x^2 - 12x + 15 \geq -1$

$\Rightarrow x^2 - 6x + 8 \geq 0$

$\Rightarrow (x-4)(x-2) \geq 0$

$\Rightarrow x \in (-\infty, 2] \cup [4, \infty)$

4. i.e. $\alpha x^2 + 6x - 8 = 0 \dots(1)$

& $-8x^2 + 6x + \alpha = 0 \dots(2)$

have a common root.

solving (1) & (2) for common root

$(1) - (2)$

$(\alpha + 8)x^2 = (8 + \alpha) \Rightarrow x = \pm 1$

so from (1) $\alpha = 2, 14$

if both root are common

$\frac{\alpha}{-8} = 1 \Rightarrow \alpha = -8$

so $\alpha = \{2, 14, -8\}$

5. $x^2 + xy + xz = 18$

$\Rightarrow x^2 + x(y+z) = 18 \dots\dots(1)$

$y^2 + yz + yx + 12 = 0$

$\Rightarrow y^2 + y(z+x) = -12 \dots\dots(2)$

$z^2 + zx + zy = 30$

$\Rightarrow z^2 + z(x+y) = 30$

Adding equation (1), (2), (3)

$x^2 + y^2 + z^2 + 2xy + 2yz + 2zx = 36$

$(x+y+z)^2 = 36$

$x+y+z = \pm 6$

Case-1 : $x+y+z = 6$

from Equ. (1)

$x^2 + x(6-x) - 18 = 0$

$x^2 + 6x - x^2 = 18$

$x = 3 \therefore x = 3, y = -2$

from Equ. (2) $\Rightarrow 2 = 6 - 1 = 5$

$y^2 + y(6-y) = -12$

$y = -2$

Case-2 : $x+y+z = -6$

from Equ. (1)

$x^2 + x(-6-x) = 18$

$x^2 - 6x - x^2 = 18$

$x = -3 \Rightarrow z = -x - y$

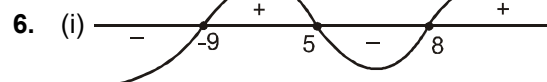
from Equ. (2) $z = -6 + 3 - 2$

$y^2 + y(-6-9) = -12 = -5$

$y^2 - 6y - y^2 = -12 \quad (x, y, z) \equiv (-3, 2, -5)$

$y = 2$

from Case-1 and Case-2, we get $(x, y, z) \equiv (3, -2, 5), (-3, 2, -5)$

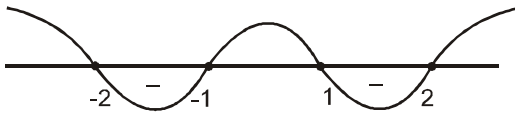


$x \in (-\infty, -9) \cup (5, \infty)$

(ii) $(x-2)^2 + 5 > 0$ so $x \in \mathbb{R}$

(iii) $(x^2 - 4)(x^2 - 1) < 0$

$$\Rightarrow (x-2)(x+2)(x-1)(x+1) < 0$$



$$x \in (-2, -1) \cup (1, 2)$$

$$(iv) \frac{3}{x-2} - 1 < 0 \Rightarrow \frac{5-x}{x-2} < 0$$

$$x \in (-\infty, 2) \cup (5, \infty)$$

7. $f(x) = x^2 - 4ax + 5a^2 - 6a$

$f(x)$ is positive for $D < 0$

$$16a^2 - 4(5a^2 - 6a) < 0$$

$$-4a^2 + 24a < 0$$

$$4a^2 - 24a > 0$$

$$4a(a-6) > 0$$

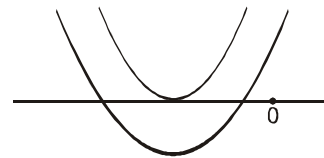
$$a > 6 \text{ or } a < 0$$

Smallest positive integer value is 7.

$$(b) \alpha - \beta = \sqrt{(\alpha + \beta)^2 - 4\alpha\beta}$$

$$= \sqrt{16a^2 - 4(5a^2 - 6a)} = \sqrt{-4a^2 + 24a}$$

$$\text{maxima at } a = 3, \alpha - \beta = \sqrt{-4 \times 3^2 + 24 \times 3} = 6$$



$$D \geq 0$$

$$\frac{-b}{2a} < 0 \quad f(0) > 0$$

$$(a+1)^2 - 9a + 5 \geq 0$$

$$a^2 - 7a + 6 \geq 0$$

$$a \in (-\infty, 1] \cup [6, \infty)$$

$$\frac{-b}{2a} < 0 \quad \text{given}$$

$$-(a+1) < 0$$

$$a+1 > 0$$

$$a > -1$$

$$f(0) > 0$$

$$9a - 5 > 0$$

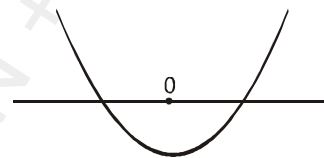
$$a > \frac{5}{9} \quad \therefore a \in \left(\frac{5}{9}, 1\right] \cup [6, \infty)$$

is the final solution

4. $3x^2 + 2(a^2 + 1)x + a^2 - 3a + 2 = 0$

for roots to be of opposite sign

derived graph is



$$f(0) < 0$$

$$a^2 - 3a + 2 < 0 \Rightarrow (a-1)(a-2) < 0$$

$$a \in (1, 2)$$

5. $x^2 - 2mx + m^2 - 1 = 0$

$$f(x) = x^2 - 2mx + m^2 - 1$$

roots lie in $(-2, 4)$

$$f(-2) > 0 \text{ \& } f(4) > 0$$

$$D > 0$$

$$f(-2) = 4 + 4m + m^2 - 1 > 0$$

$$m^2 + 4m + 3 > 0$$

$$(m+1)(m+3) > 0$$

$$m > -1 \text{ or } m < -3 \quad \dots(1)$$

$$f(4) > 0$$

$$f(4) = 16 - 8m + m^2 - 1 > 0$$

$$m^2 - 8m + 15 > 0$$

$$(m-3)(m-5) > 0$$

$$m < 3 \text{ or } m > 5 \quad \dots(2)$$

$$D > 0$$

$$4m^2 - 4(m^2 - 1) > 0$$

$$4 > 0$$

using (1), (2) & (3)

$$m \in \mathbb{R} \quad \dots(3)$$

$$\text{so } m \in (-1, 3)$$

6. $x^3 - 5x^2 + 6x - 3 = 0$

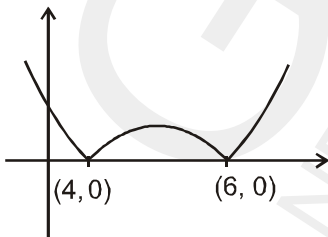
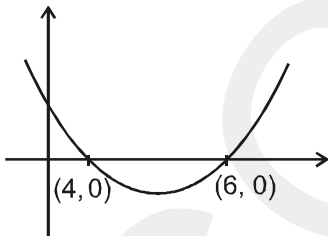
α, β, γ are root of equation

$\alpha + 1, \beta + 1, \gamma + 1$ are roots of newer equation

$$x^3 - (\alpha + \beta + \gamma + 3)x^2 + [(\alpha + 1)(\beta + 1) + (\beta + 1)(\gamma + 1) + (\gamma + 1)(\alpha + 1)]x - (\alpha + 1)(\beta + 1)(\gamma + 1)$$

DPP NO. - 14

1. $y = x^2 - 10x + 24$ now $y = |x^2 - 10x + 24|$



2. $3^{2(x^2-x-6)} - 2 \cdot 3^{(x^2-x-6)} + 1 = 0$

$$\Rightarrow 3^{(x^2-x-6)} = 1$$

$$\Rightarrow x^2 - x - 6 = 0$$

$$\Rightarrow (x-3)(x+2) = 0$$

$$\Rightarrow x = -2, 3$$

3. $x^2 + 2(a+1)x + 9a - 5 = 0$

for both roots to be $-ve$

desired graph is

$$\alpha + \beta + \gamma = 5, \alpha\beta + \beta\gamma + \gamma\alpha = 6$$

$$\alpha\beta\gamma = 3$$

$$x^3 - (8)x^2 + [\alpha\beta + \beta\gamma + \gamma\alpha + 2(\alpha + \beta + \gamma)]x - (\alpha\beta\gamma + \alpha\beta + \beta\gamma + \gamma\alpha + \alpha + \beta + \gamma + 1) = 0$$

$$= x^3 - 8x^2 + [6 + 10]x - [3 + 6 + 5 + 1] = 0$$

$$x^3 - 8x^2 + 16x - 15 = 0$$

7. $(p - 3)x^2 - 2px + 5p = 0$
 $f(x) = (p - 3)x^2 - 2px + 5p$
 for real & positive
 $D \geq 0$
 $4p^2 - 20p(p - 3) \geq 0$
 $4p^2 - 20p^2 + 60p \geq 0$
 $-16p^2 + 60p \geq 0$
 $4p(-4p + 15) \geq 0$
 $4p(4p - 15) \leq 0$

$$0 \leq p \leq \frac{15}{4}, p \in \left(0, \frac{15}{4}\right] \quad \dots(1)$$

Case-I : if $p - 3 > 0, p > 3$

$$f(0) > 0, 5p > 0 \quad \frac{-b}{2a} > 0, \frac{p}{p-3} > 0$$

$$p > 3 \text{ or } p < 0$$

$$p \in (3, \infty) \quad \dots(2)$$

Case-II : $p < 3$

$$f(0) < 0, p < 0, \frac{-b}{2a} > 0 \quad \frac{p}{p-3} > 0$$

$$p > 3 \text{ or } p < 0$$

$$p \in (-\infty, 0) \quad \dots(3)$$

$$p \in \left[3, \frac{15}{4}\right]$$

4. $a\left(\frac{x}{1-x}\right)^2 + b\left(\frac{x}{1-x}\right) + c = 0$

$$\Rightarrow \frac{x}{1-x} = \alpha$$

$$x = \alpha - \alpha x$$

$$x = \frac{\alpha}{1+\alpha}$$

5. $x^3 - px^2 + qx - r = 0$

α, β, γ are root of equation

$$\sum \alpha^2\beta = \alpha^2\beta + \alpha^2\gamma + \beta^2\alpha + \beta^2\gamma + \gamma^2\alpha + \gamma^2\beta$$

$$= (\alpha^2\beta + \alpha^2\gamma + \alpha\beta\gamma) + (\beta^2\alpha + \beta^2\gamma + \alpha\beta\gamma) + (\gamma^2\alpha + \gamma^2\beta + \alpha\beta\gamma) - 3\alpha\beta\gamma$$

$$= \alpha(\alpha\beta + \beta\gamma + \alpha\gamma) + \beta(\beta\alpha + \beta\gamma + \alpha\gamma) + \gamma(\alpha\beta + \beta\gamma + \gamma\alpha) - 3\alpha\beta\gamma$$

$$= (\alpha\beta + \beta\gamma + \gamma\alpha)(\alpha + \beta + \gamma) - 3\alpha\beta\gamma$$

$$= qp - 3r$$

6. α, β, γ are roots are roots of $x^3 - px^2 + qx - r = 0$

$$\alpha + \beta + \gamma = p, \sum \alpha\beta = q, \alpha\beta\gamma = r$$

$$\left(\frac{1}{\alpha^2} + \frac{1}{\beta^2} + \frac{1}{\gamma^2}\right) = \frac{\alpha^2\beta^2 + \beta^2\gamma^2 + \gamma^2\alpha^2}{\alpha^2\beta^2\gamma^2}$$

$$= \frac{(\alpha\beta + \beta\gamma + \gamma\alpha)^2 - 2[\alpha\beta^2\gamma + \gamma\alpha^2\beta + \alpha\beta\gamma^2]}{\alpha^2\beta^2\gamma^2}$$

$$= \frac{q^2 - 2rp}{r^2}$$

7. $(x - 3k)(x - k - 3) < 0$

$$x \in [1, 3]$$

$$\text{for } x = 1, (1 - 3k)(1 - k - 3) < 0$$

$$(3k - 1)(k + 2) < 0$$

$$k \in \left(-2, \frac{1}{3}\right)$$

$$\text{for } x = 3, (3 - 3k)(-k) < 0$$

$$(k - 1)k < 0$$

$$k \in (0, 1)$$

$$\text{so } k \in \left(0, \frac{1}{3}\right)$$

DPP NO. - 15

1. $f(x) = x^2 + 2ax + b$

$$\frac{-D}{4a} = \frac{-(4a^2 - 4b)}{4}$$

$$g(x) = cx^2 + 2dx + 1$$

$$\frac{-D}{4a} = \frac{-(4d^2 - 4c)}{4c}$$

$$\frac{4a^2 - 4b}{4} = -\left(\frac{4d^2 - 4c}{4c}\right) \Rightarrow a^2 - b = \frac{-d^2 + c}{c}$$

$$a^2c - bc = -d^2 + c$$

$$a^2c + d^2 = bc + c$$

2. Sum of roots = $-b/2a$

$$\text{since } |OA'| = |OB|$$

$$OA' = -OB$$

hence sum of roots of $f(x) = 0$ & $g(x) = 0$ is zero.

3. $(g(x))^2 + mg(x) + 4 = 0$

$$m^2 - 16 > 0$$

$$m \in (-\infty, -4) \cup (4, \infty)$$

$$|OA'| = |AA'| = 1$$

$$|OA'| = |OB| = 1 = |BB'|$$

if $y = g(x)$ to have real roots $y > -1$

$$m \in (5, \infty)$$

DPP NO. - 16

1. $|x^2 - 2x - 3| = m$

$$x^2 - 2x - 3 - m = 0$$

$$\text{or } x^2 - 2x - 3 + m = 0$$

if equation has 4 solutions

$$4 + 4(3 + m) > 0 \text{ \& } 4 - 4(m - 3) > 0$$

$$4 + m > 0 \text{ \& } -4m + 16 > 0$$

$$m > -4 \text{ \& } m < 4$$

$$\text{Since } |x^2 - 2x - 3| = m$$

so m should be positive

$$\text{hence } m \in (0, 4)$$

6. $\frac{-1}{|x|-2} \geq 1 \Rightarrow \frac{-1}{|x|-2} - 1 \geq 0$
 $\Rightarrow \frac{-1-|x|+2}{|x|-2} \geq 0 \Rightarrow \frac{1-|x|}{|x|-2} \geq 0$
 $\Rightarrow \frac{|x|-1}{|x|-2} \leq 0$
 $\Rightarrow 1 \leq |x| < 2$
 $\Rightarrow |x| \geq 1 \quad \& \quad |x| < 2$
 $\Rightarrow x \in (-\infty, -1] \cup [1, \infty) \cap x \in (-2, 2)$
 $\Rightarrow x \in (-2, -1] \cup [1, 2)$

7. $\frac{|x+3|+x}{x+2} > 1$
 $\Rightarrow \frac{|x+3|+x-x-2}{x+2} > 0 \Rightarrow \frac{|x+3|-2}{x+2} > 0$

Case-I : $x \leq -3$ (1)

$\frac{-x-3-2}{x+2} > 0$
 $\Rightarrow \frac{-x-5}{x+2} > 0$
 $\Rightarrow \frac{x+5}{x+2} < 0$
 $\Rightarrow -5 < x < -2$
 $\Rightarrow x \in (-5, -2)$ (2)
 $(1) \cap (2) \Rightarrow x \in (-5, -3]$ (A)

Case-II : $x > -3$ (3)

$x > -3$
 $\frac{x+3-2}{x+2} > 0$
 $\frac{x+1}{x+2} > 0$
 $x \in (-\infty, -2) \cup (-1, \infty)$ (4)
 $(3) \cap (4) \Rightarrow x \in (-3, -2] \cup (-1, \infty)$ (B)
 $\therefore (A) \cup (B) \Rightarrow x \in (-5, -2) \cup (-1, \infty)$

8. $||x-2|-1| \geq 3$
 $\Rightarrow |x-2|-1 \leq -3$ or $|x-2|-1 \geq 3$
 $\Rightarrow |x-2| \leq -2$ or $|x-2| \geq 4$
 $\Rightarrow x \in \phi$ or $x-2 \geq -4$ or $x-2 \geq 4$
 or $x \leq -2$ or $x \geq 6$
 \therefore Ans. $(-\infty, -2] \cup [6, \infty)$

9. $|(x^2+2x+2) + (3x+7)| < |x^2+2x+2| + |3x+7|$
 $\underbrace{(x^2+2x+2)}_{+ve \ D < 0} (3x+7) < 0$
 $[\because |x+y| < |x| + |y| \Rightarrow xy < 0]$
 $\Rightarrow 3x+7 < 0 \Rightarrow x < -\frac{7}{3}$

10. $|x^2-1| + |x^2-4| \leq 3$
Case-I : When $x^2 < 1$
 $\Rightarrow x \in (-1, 1)$ (i)
 $-(x^2-1) - (x^2-4) \leq 3$

$\Rightarrow -2x^2 \leq -2 \Rightarrow x^2 \geq 1$
 $\Rightarrow x \in (-\infty, -1] \cup [1, \infty)$ (ii)
 $(i) \cap (ii) \Rightarrow x \in \phi$

Case-II : $1 \leq x^2 \leq 4$
 $\Rightarrow 1 \leq |x| \leq 2 \Rightarrow |x| \geq 1 \quad \& \quad |x| \leq 2$
 $\Rightarrow x \in (-\infty, -1] \cup [1, \infty) \cap [-2, 2]$
 $\Rightarrow x \in (-2, -1] \cup [1, 2]$ (iii)
 $x^2 - 1 - x^2 + 4 \leq 3$
 $3 \leq 3$ which is true.
 $\therefore x \in [-2, -1] \cup [1, 2]$ (iv)

Case-III : $x^2 > 4$
 $\Rightarrow |x| > 2 \Rightarrow x \in (-\infty, -2) \cup (2, \infty)$ (v)
 $x^2 - 1 + x^2 - 4 \leq 3$
 $\Rightarrow 2x^2 - 5 \leq 3$
 $\Rightarrow 2x^2 \leq 8$
 $\Rightarrow x^2 \leq 4$
 $\Rightarrow x \in [-2, 2]$ (vi)
 $(v) \cap (vi) \Rightarrow x \in \phi$
 \therefore Ans. $x \in [-2, -1] \cup [1, 2]$

11. $|x^2+3x| + x^2 - 2 \geq 0$
 $\Rightarrow |x(x+3)| + x^2 - 2 \geq 0$
Case-I $x < -3$ (i)
 $\Rightarrow x(x+3) + x^2 - 2 \leq 0$
 $\Rightarrow x^2 + 3x + x^2 - 2 \geq 0$
 $\Rightarrow 2x^2 + 4x - x - 2 \geq 0$
 $\Rightarrow 2x(x+2) - 1(x+2) \geq 0$
 $\Rightarrow (2x-1)(x+2) \geq 0$
 $\Rightarrow x \in (-\infty, -2] \cup [1/2, \infty)$ (ii)
 $(i) \cap (ii) \Rightarrow x \in (-\infty, -3)$ (A)

Case-II : $-3 \leq x < 0$ (iii)
 $-x(x+3) + x^2 - 2 \geq 0$
 $\Rightarrow -x^2 - 3x + x^2 - 2 \leq 0$
 $\Rightarrow 3x + 2 \leq 0$
 $\Rightarrow x \leq -\frac{2}{3}$ (iv)
 $(iii) \cap (iv) \Rightarrow x \in \left[-3, -\frac{2}{3}\right]$ (B)

Case-III : $x \geq 0$ (v)
 $x^2 + 3x + x^2 - 2 \geq 0$
 $\Rightarrow x \in (-\infty, -2] \cup \left[\frac{1}{2}, \infty\right)$ (C)

Ans. $(A) \cup (B) \cup (C) \Rightarrow x \in \left(-\infty, -\frac{2}{3}\right] \cup \left[\frac{1}{2}, \infty\right)$

12. $||x|-1| < |1-x|, x \in \mathbb{R}$
 +ve +ve
 squaring both sides,
 $\Rightarrow (|x|-1)^2 < (1-x)^2$
 $\Rightarrow x^2 + 1 - 2|x| < 1 + x^2 - 2x$
 $\Rightarrow |x| > x$
 $\Rightarrow x < 0$
 $\Rightarrow x \in (-\infty, 0)$

13. $|x^2+4x+3| + 2x+5 = 0$
 $\Rightarrow |(x+1)(x+3)| + 2x+5 = 0$
Case-I : $x < -3$
 $+(x+1)(x+3) + 2x+5 = 0$

$$x^2 + 6x + 8 = 0$$

$$\Rightarrow (x + 4)(x + 2) = 0$$

$$\Rightarrow x = -2, -4$$

$$\therefore x < -3 \Rightarrow x = -4$$

Case-II : $-3 \leq x < -1$

$$-(x + 1)(x + 3) + 2x + 5 = 0$$

$$-x^2 - 4x - 3 + 2x + 5 = 0$$

$$-x^2 - 2x + 2 = 0$$

$$x^2 + 2x - 2 = 0$$

$$\Rightarrow x = \frac{-2 \pm \sqrt{4+8}}{2} = \frac{-2 \pm 2\sqrt{3}}{2} = -1 \pm \sqrt{3}$$

$$\therefore -3 \leq x < -1$$

$$\therefore x = -1 - \sqrt{3}$$

Case-III : $x \geq -1$

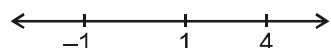
$$\left. \begin{aligned} x^2 + 4x + 3 + 2x + 5 = 0 \\ \Rightarrow x^2 + 6x + 8 = 0 \\ \Rightarrow x = -2, -4 \end{aligned} \right\} \cap \Rightarrow x \in \phi$$

$$\therefore \text{Ans. } x \in \{-4, -1 - \sqrt{3}\}$$

14. $|x^2 - 3x - 4| = 9 - |x^2 - 1|$

$$\Rightarrow |x^2 - 3x - 4| + |x^2 - 1| = 9$$

$$\Rightarrow |(x - 4)(x + 1)| + |(x + 1)(x - 1)| = 9$$



Case-I : $x < -1$

$$x^2 - 3x - 4 + x^2 - 1 = 9$$

$$\Rightarrow 2x^2 - 3x - 5 = 9$$

$$\Rightarrow 2x^2 - 3x - 14 = 0$$

$$\Rightarrow 2x^2 - 7x + 4x - 14 = 0$$

$$\Rightarrow x(2x - 7) + 2(2x - 7) = 0$$

$$\Rightarrow x = -2, 7/2$$

$$\therefore x < -1 \quad \therefore x = -2$$

Case-II : $-1 \leq x < 1$

$$-(x^2 - 3x - 4) - (x^2 - 1) = 9$$

$$\Rightarrow -x^2 - 3x + 4 - x^2 + 1 = 9$$

$$\Rightarrow -2x^2 + 3x + 5 = 9$$

$$\Rightarrow -2x^2 + 3x - 4 = 0$$

$$\Rightarrow 2x^2 - 3x + 4 = 0$$

$$\Rightarrow D < 0 \quad \therefore \text{it has no real roots.}$$

$$\therefore x \in \phi$$

$$1 \leq x < 4$$

$$-(x^2 - 3x - 4) + x^2 - 1 = 9$$

$$\Rightarrow -x^2 + 3x + 4 + x^2 - 1 = 9$$

$$\Rightarrow 3x + 3 = 9$$

$$\Rightarrow 3x = 6$$

$$\Rightarrow x = 2 \in [1, 4)$$

$$\therefore x = 2$$

Case-IV : $x \geq 4$

$$x^2 - 3x - 4 + x^2 - 1 = 9$$

$$\Rightarrow 2x^2 - 3x - 5 = 9$$

$$\Rightarrow 2x^2 - 3x - 5 = 9$$

$$\Rightarrow 2x^2 - 7x + 4x - 14 = 0$$

$$\Rightarrow x(2x - 7) + 2(2x - 7) = 0$$

$$\Rightarrow (x + 2)(2x - 7) = 0$$

$$\Rightarrow x = -2, 7/2$$

$$\therefore x \geq 4$$

$$\therefore x \in \phi$$

$$\therefore x \in \{-2, 2\}$$

15. $|f(x) - g(x)| < |f(x)| + |g(x)|$

Square both sides.

$$\Rightarrow (f(x) - g(x))^2 < (|f(x)| + |g(x)|)^2$$

$$\Rightarrow f^2(x) + g^2(x) - 2f(x) \cdot g(x) < f^2(x) + g^2(x) + 2|f(x) \cdot g(x)|$$

$$\Rightarrow -2f(x) \cdot g(x) < 2|f(x) \cdot g(x)|$$

$$\Rightarrow |f(x) \cdot g(x)| > -f(x) \cdot g(x)$$

$$\Rightarrow f(x) \cdot g(x) > 0$$

$$\Rightarrow (x - 3)(4 - x) > 0$$

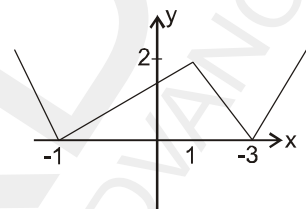
$$\Rightarrow (x - 3)(x - 4) < 0$$

$$\Rightarrow x \in (3, 4)$$

DPP NO. - 18

1. for two solution

$$||x - 1| - 2| = \lambda \text{ graph of } f(x) = ||x - 1| - 2|$$



$$\lambda \in (2, \infty) \cup \{0\}$$

2. For three solution

$$\lambda = 2$$

3. for four solution

$$\lambda \in (0, 2)$$

so integral values of $\lambda = 1$

4. α, β, γ are roots of equation

$$x^3 - px^2 + qx - r = 0$$

$$\alpha + \beta + \gamma = p$$

$$\alpha\beta + \beta\gamma + \alpha\gamma = q$$

$$\alpha\beta\gamma = r$$

$$\sum \frac{\alpha\beta}{\gamma} = \frac{\alpha\beta}{\gamma} + \frac{\beta\gamma}{\alpha} + \frac{\alpha\gamma}{\beta} = \frac{\alpha^2\beta^2 + \beta^2\gamma^2 + \alpha^2\gamma^2}{\alpha\beta\gamma} =$$

$$\frac{(\alpha\beta + \beta\gamma + \alpha\gamma)^2 - 2}{\alpha\beta\gamma} = \frac{q^2 - 2pr}{r}$$

5. $S_1 : ax^2 + bx + c = 0$ ($a \neq 0$)

if $a + b + c = 0$ then one root is 1

$$\text{product of roots} = \frac{c}{a}$$

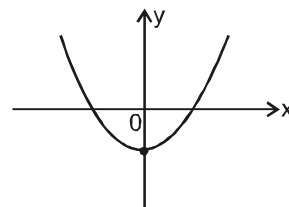
$$\text{so another root} = \frac{c}{a}$$

$S_2 : f(x) = ax^2 + bx + c$ ($a \neq 0$)

it has finite minimum value of graph is

upward parabola

roots are of opposite sign



so $f(0) < 0$

S_3 : α is repeated root of

$$ax^2 + bx + c = 0$$

$$\text{so } ax^2 + bx + c = a(x - \alpha)^2$$

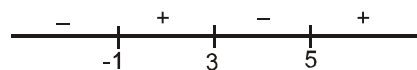
$$S_n : ax^2 + bx + c = 0 \quad (a \neq 0)$$

Irrational roots occur in conjugate pair only if a, b, c are rational.

6. α, β are roots of $x^2 + \alpha x + \beta = 0$ is
 $\alpha + \beta = -\alpha \dots(1)$ and $\alpha\beta = \beta \dots(2)$
 from (1) & (2) $\alpha = 1, \beta = -2$
 Now $||x + 2| - 1| < 1$
 $\Rightarrow -1 < |x + 2| - 1 < 1$
 $0 < |x + 2| < 2$
 $\Rightarrow -2 < x + 2 < 2$ and $x \neq -2$
 $x \in (-4, 0) - \{-2\}$

7. $(a - 5)x^2 + (\sqrt{4a - a^2})x + (a^2 - 2a - 3) = 0$
 for defining equation $4a - a^2 \geq 0$
 $a(a - 4) \leq 0$
 $a \in [0, 4] \dots(1)$
 roots are of opposite sign

$$\text{so } \frac{a^2 - 2a - 3}{a - 5} < 0 \Rightarrow \frac{(a - 3)(a + 1)}{a - 5} < 0$$



$$\Rightarrow a \in (-\infty, -1) \cup (3, 5) \dots(2)$$

from (1) & (2)
 $a \in (3, 4]$

8. $\frac{ax^2 + 3x + 4}{x^2 + 2x + 2} - 5 < 0 \Rightarrow \frac{(a - 5)x^2 - 7x - 6}{x^2 + 2x + 2} < 0$

but $x^2 + 2x + 2$ is always positive
 so $(a - 5)x^2 - 7x - 6 < 0 \quad \forall x \in \mathbb{R}$
 so $a - 5 < 0 \Rightarrow a < 5$
 and $D = 49 - 4(a - 5)(-6) < 0$
 $49 + 24(a - 5) < 0$
 $24a < 71$

$$a < \frac{71}{24}$$

$$\text{so } a < \frac{71}{24}$$

Max. Integral value of $a = 2$

DPP NO. - 19

1. $n(P) = 25\%, n(C) = 15\%$
 $n(P^c \cap C^c) = 65\%, n(P \cap C) = 2000$
 Since $n(P^c \cap C^c) = 65\%$
 $\therefore n(P \cup C)^c = 65\% \therefore n(P \cup C) = 35\%$ (2 is correct)
 Now $n(P \cup C) = n(P) + n(C) - n(P \cap C)$
 $\therefore 35 = 25 + 15 - n(P \cap C) \Rightarrow n(P \cap C) = 40 - 35 = 5$
 Thus $n(P \cap C) = 5\%$
 But $n(P \cap C) = 2000$
 $\therefore 5\%$ of total = 2000
 \therefore total number of families = $\frac{2000 \times 100}{5} = 40000$

$$\therefore n(P \cup C) = 35\%$$

Total number of families = 40,000 (3 is correct)
 and $n(P \cap C) = 5\%$

2. $A \cap (B \cup A)' = A \cap (B' \cap A') = (A \cap B') \cap (A \cap A') = (A \cap B') \cap \phi = \phi$.
3. Let number of people teaching mathematics, physics, both physics and mathematics, physics or mathematics are $n(m), n(p), n(p \cap m), n(p \cup m)$ respectively.
 $\therefore n(m \cup p) = n(m) + n(p) - n(p \cap m)$
 $20 = 12 + n(p) - 4$
 $\therefore n(p) = 12$

4. 3, 9, 999
 $999 = 3 + (n - 1)6$
 $\frac{996}{6} = (n - 1) \Rightarrow 166$
 $n = 167$
 sum = $\frac{167}{2} (3 + 999)$
 $\Rightarrow \frac{167}{2} (1002) \Rightarrow (167) (501)$
 $= 83667$

5. $a_1 + a_2 + a_4 + \dots + a_{200} = \alpha$
 $a_1 + a_3 + a_5 + \dots + a_{199} = \beta$

 $100d = \alpha - \beta$
 $d = \frac{\alpha - \beta}{100}$

6. $\frac{S_{n1}}{S_{n2}} = \frac{3n - 13}{5n + 21} \Rightarrow \frac{2a_1 + (n - 1)d}{2a_2 + (n - 1)d} = \frac{3n - 13}{5n + 21}$

$$\frac{a_1 + \left(\frac{n - 1}{2}\right)d_1}{a_2 + \frac{(n - 1)d_2}{2}} = \frac{3n - 13}{5n + 21}$$

$$\text{Now } T_{24} = \frac{n - 1}{2} = 23$$

$$n = 47$$

$$\frac{a_1 + 23d_1}{a_2 + 23d_2} = \frac{3.47 - 17}{5.47 + 21} = \frac{1}{2}$$

7. $a - d, a, a + d$
 $3a = 9 \Rightarrow a = 3$
 $(a - d)^2 + a^2 + (a + d)^2 = 35$
 $3a^2 + 2d^2 = 35$
 $d^2 = 4$
 $d = 2, -2$
 $S_n = \frac{n}{2} [2 + (n - 1).2] \Rightarrow n^2$
 $S_n = \frac{n}{2} [10 + (n - 1)(-2)]$
 $= \frac{n}{2} [12 - 2n] = n(6 - n)$

DPP NO. - 20

1 to 3. a, b, c, d

18, p, $\frac{p}{2}$, $\frac{p}{4}$

$2p = \frac{p}{2} + 18 \Rightarrow p = 12$

18, 12, 6, 3

a b c d

c + d = 9

12 A₁ A₂ A₃ 6

$d = \frac{6-12}{4} \Rightarrow -\frac{3}{2}$

$A_3 = 6 - d = 6 + \frac{3}{2} = \frac{15}{2}$

$k_1 C A_1 A_2 A_3 A_4 k_2 d \quad k_2 = 64k_1$

$r = \left(\frac{k_2 d}{k_1 c}\right)^{1/5}$

$r = (32)^{1/5} = 2$

4. $\frac{a(1-r^3)}{a(1-r^6)} = \frac{125}{152} \Rightarrow \frac{1}{1+r^3} = \frac{125}{152}$

$152 = 125 + 125r^3$

$r = \frac{3}{5}$

5. $\frac{3}{4}, \frac{2}{3}, \frac{7}{12}$ A.P.

$a = \frac{3}{4} \quad d = \frac{2}{3} - \frac{3}{4} = -\frac{1}{12}$

$T_{61} = a + 60d$

$= \frac{3}{4} + 60 \left[-\frac{1}{12}\right] = -5 + \frac{3}{4} = -\frac{17}{4}$

T_{61} of an H.P. = $-\frac{4}{17}$

6. $200 < \frac{9}{2}(a_1 + a_9) < 220$

$\frac{400}{9} < a_1 + a_9 < \frac{400}{9}$

$\frac{400}{9} < a_1 + a_1 + 8d < \frac{440}{9}$

$\frac{200}{9} < a_1 + 4d < \frac{220}{9}$

$22 < a_1 + 4d < 24.4$

$a_1 + 4d = 23$ or 24

$a + d = 12$ or 12

 $3d = 12$

$d = 4$

$a = 8 \quad 8, 12, 16, \dots$

7. $x_1 + x_2 = 3 \quad x_3 + x_4 = 12$

$x_1 x_2 = A \quad x_3 x_4 = B$

$x_1 x_2 x_3 x_4 \rightarrow$ G.P.

$a \quad ar \quad ar^2 \quad ar^3 \rightarrow |r| > 1$

$a(1+r) = 3$

$ar^2(1+r) = 12$

 $r = 2, -2$ Hence $r = 2$

$a = 1$

$A = a \cdot ar = a^2 r = 2$

$B = a^2 r^5 = 2^5 = 32$